



Computação Gráfica

Computer Graphics

Engenharia Informática (11569) – 3º ano, 2º semestre

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Chap. 4 – Windows and Viewports



Outline

....:

- Basic definitions in 2D:
 - Global coordinates (scene domain): continuous domain
 - Screen coordinates (image domain): discrete domain
- Window-viewport transformation
- Window-viewport transformation in OpenGL
- Geometric transformations in OpenGL/GLM
- Graphics pipeline (or rendering pipeline)
- Mapping a scene into various viewports
- Avoiding image distortion
- OpenGL examples

Definitions

scene domain (\mathbb{R}^2)

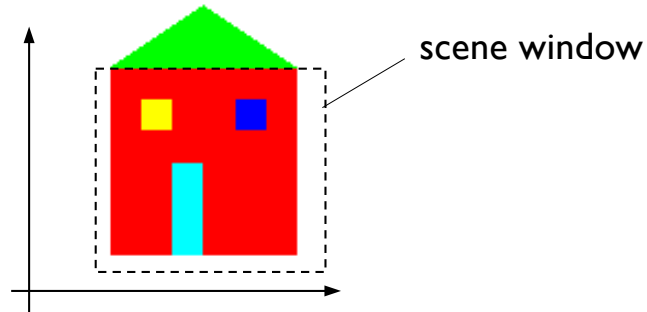
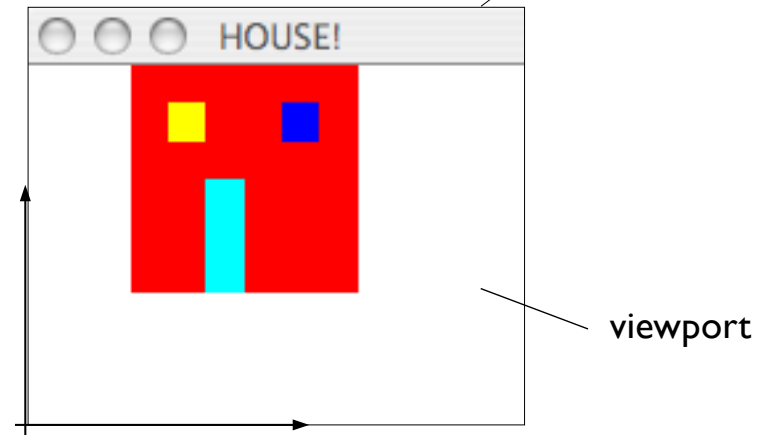


image domain
(screen)

screen window



Global (or world) coordinate system (or scene domain)

- is associated with the scene domain (or application domain)
- is where geometric objects lie in
- is where the geometry of each scene's object is defined
- the scene domain is continuous (e.g., \mathbb{R}^2)

Scene window (scene sub-domain)

- rectangular scene sub-domain whose contents we intend to display on screen

Image coordinate system (or image domain)

- is associated with a screen window
- screen space where the raster image is displayed (e.g., 500x500 pixels)
- a screen window may comprise various viewports, which may overlap
- the image domain is discrete (pixels)

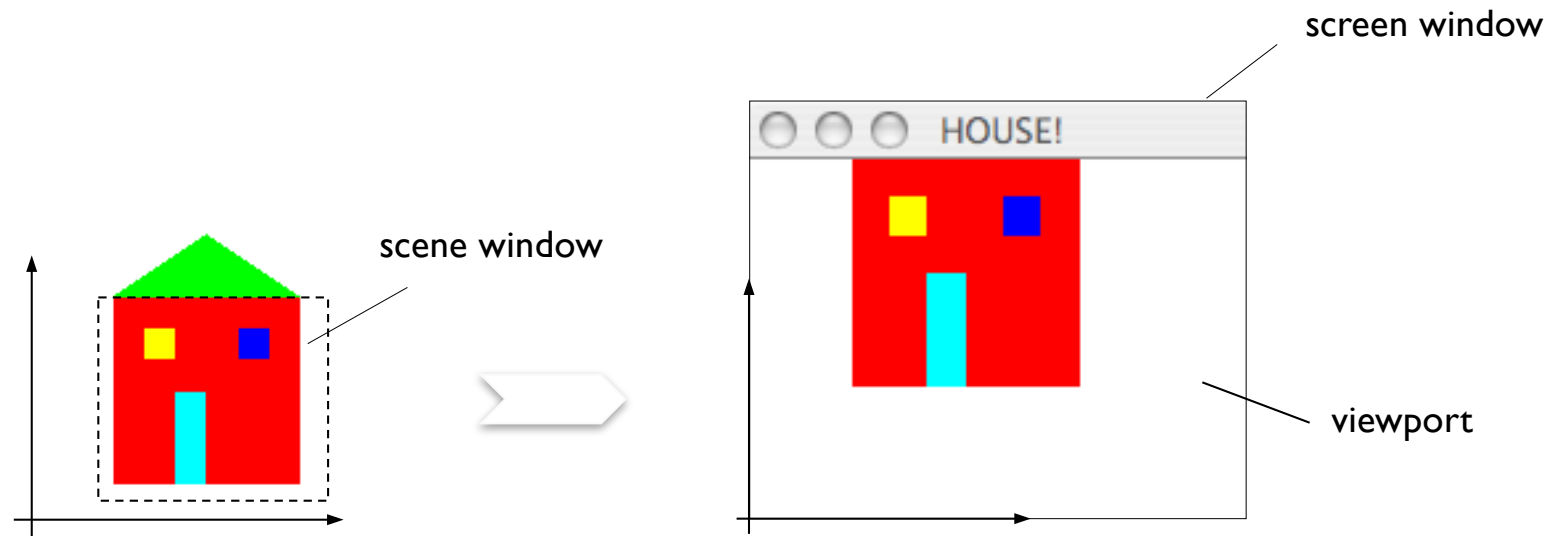
Viewport (image sub-domain)

- part of the screen window where the image is rendered

Window-viewport transformation

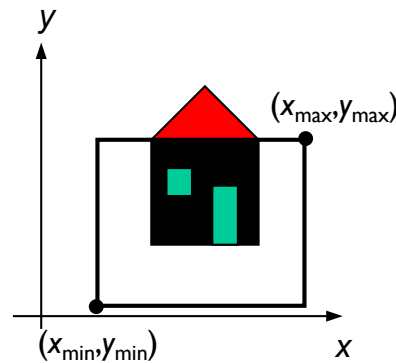
We need an automated process:

- To map a scene window (world coordinates) into a viewport (screen coordinates), the so-called window-viewport transformation.
- Thus, in principle, the same scene can be mapped into different viewports, no matter they belong to the same screen window or not.

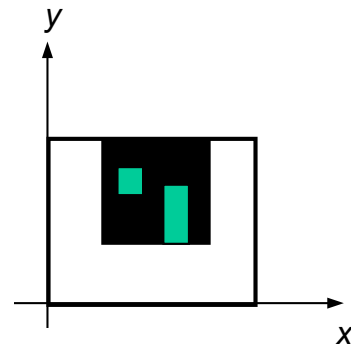


Window-viewport transformation

- This operation is performed in an automated manner by the graphics system.
- It involves 3 geometric transformations: translation in global coordinates, scaling, and translation in screen coordinates.

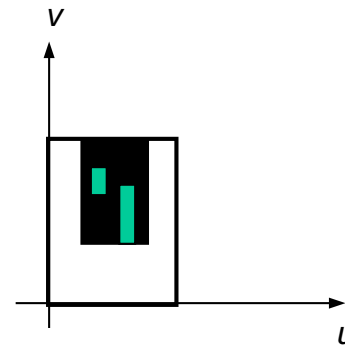


window in global or world coordinates (scene domain)



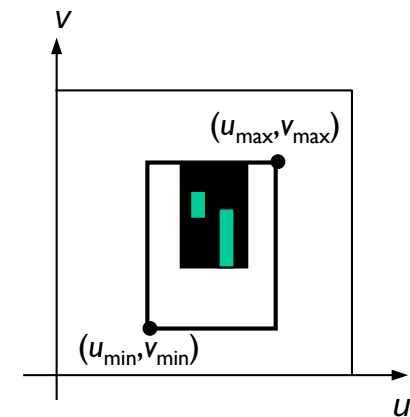
window translated to the origin

$$T(-x_{\min}, -y_{\min})$$



viewport in image coordinates

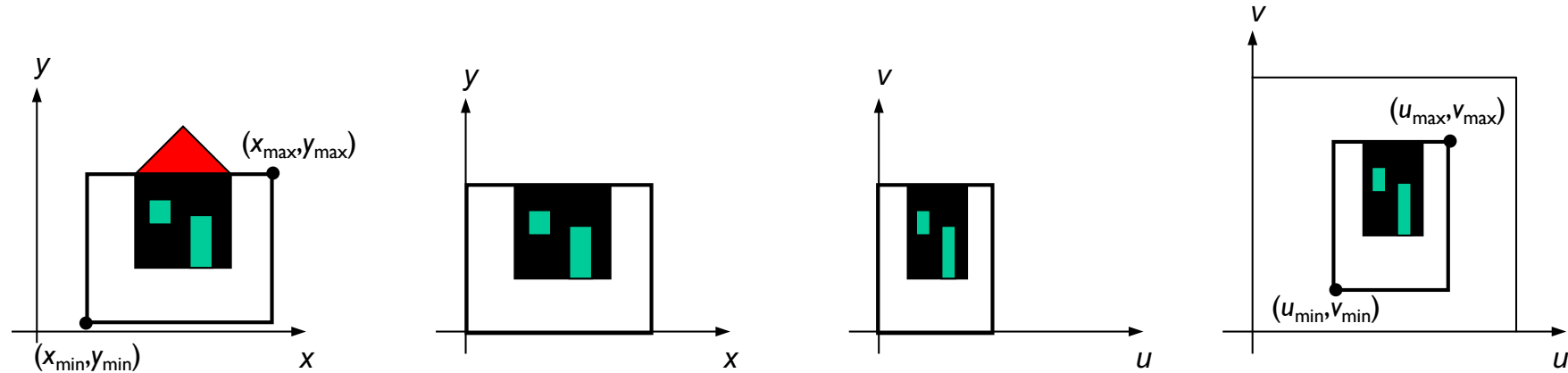
$$S\left(\frac{u_{\max} - u_{\min}}{x_{\max} - x_{\min}}, \frac{v_{\max} - v_{\min}}{y_{\max} - y_{\min}}\right)$$



viewport translated to its pre-defined position

$$T(u_{\min}, v_{\min})$$

Window-viewport transformation: matrix representation



$$T(-x_{\min}, -y_{\min})$$

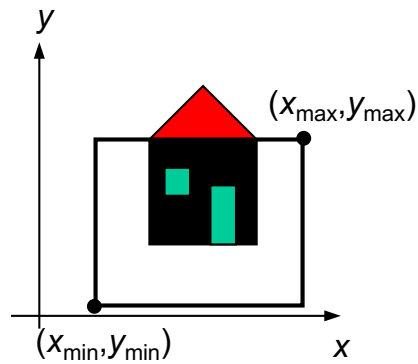
$$S\left(\frac{u_{\max} - u_{\min}}{x_{\max} - x_{\min}}, \frac{v_{\max} - v_{\min}}{y_{\max} - y_{\min}}\right)$$

$$T(u_{\min}, v_{\min})$$

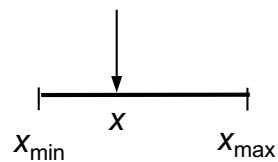
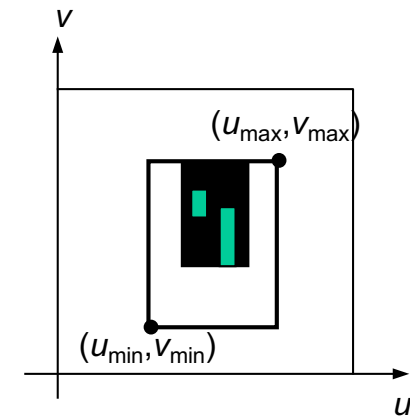
$$M_{wv} = T(u_{\min}, v_{\min}) \cdot S\left(\frac{u_{\max} - u_{\min}}{x_{\max} - x_{\min}}, \frac{v_{\max} - v_{\min}}{y_{\max} - y_{\min}}\right) \cdot T(-x_{\min}, -y_{\min})$$

$$= \begin{bmatrix} 1 & 0 & u_{\min} \\ 0 & 1 & v_{\min} \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} \frac{u_{\max} - u_{\min}}{x_{\max} - x_{\min}} & 0 & 0 \\ 0 & \frac{v_{\max} - v_{\min}}{y_{\max} - y_{\min}} & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -x_{\min} \\ 0 & 1 & -y_{\min} \\ 0 & 0 & 1 \end{bmatrix}$$

Window-viewport transformation: in more detail

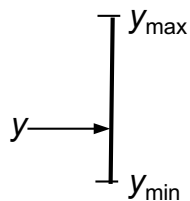
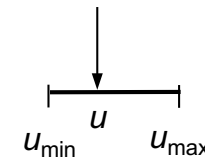


Keeping the ratio in
mapping (x,y) to (u,v)

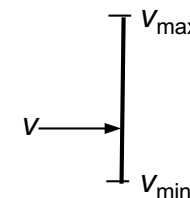


$$\frac{x - x_{\min}}{x_{\max} - x_{\min}} = \frac{u - u_{\min}}{u_{\max} - u_{\min}} \Leftrightarrow u = (x - x_{\min}) \cdot \frac{u_{\max} - u_{\min}}{x_{\max} - x_{\min}} + u_{\min}$$

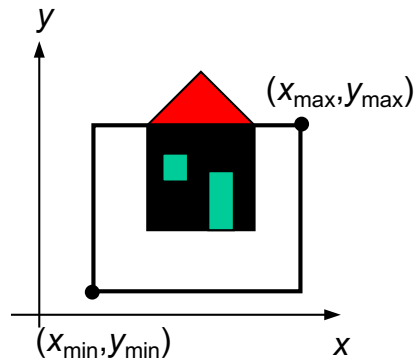
translation *scaling* *translation*



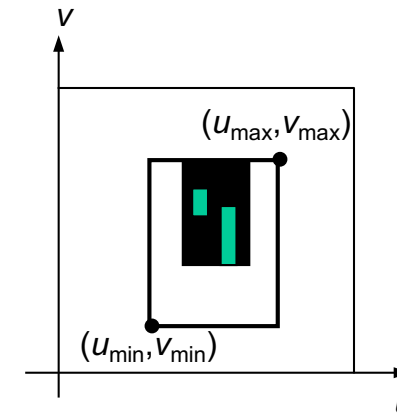
$$\frac{y - y_{\min}}{y_{\max} - y_{\min}} = \frac{v - v_{\min}}{v_{\max} - v_{\min}} \Leftrightarrow v = (y - y_{\min}) \cdot \frac{v_{\max} - v_{\min}}{y_{\max} - y_{\min}} + v_{\min}$$



Window-viewport transformation: example



window(10.0,5.0,40.0,30.0)



viewport(100,50,250,300)

$$u = (x - 10.0) \cdot \frac{250 - 100}{40.0 - 10.0} + 100 \quad \lambda_x = \frac{250 - 100}{40.0 - 10.0} = 5.0$$

$$v = (y - 5.0) \cdot \frac{300 - 50}{30.0 - 5.0} + 50 \quad \lambda_y = \frac{300 - 50}{30.0 - 5.0} = 10.0$$

Window-viewport transformation: GLM and OpenGL

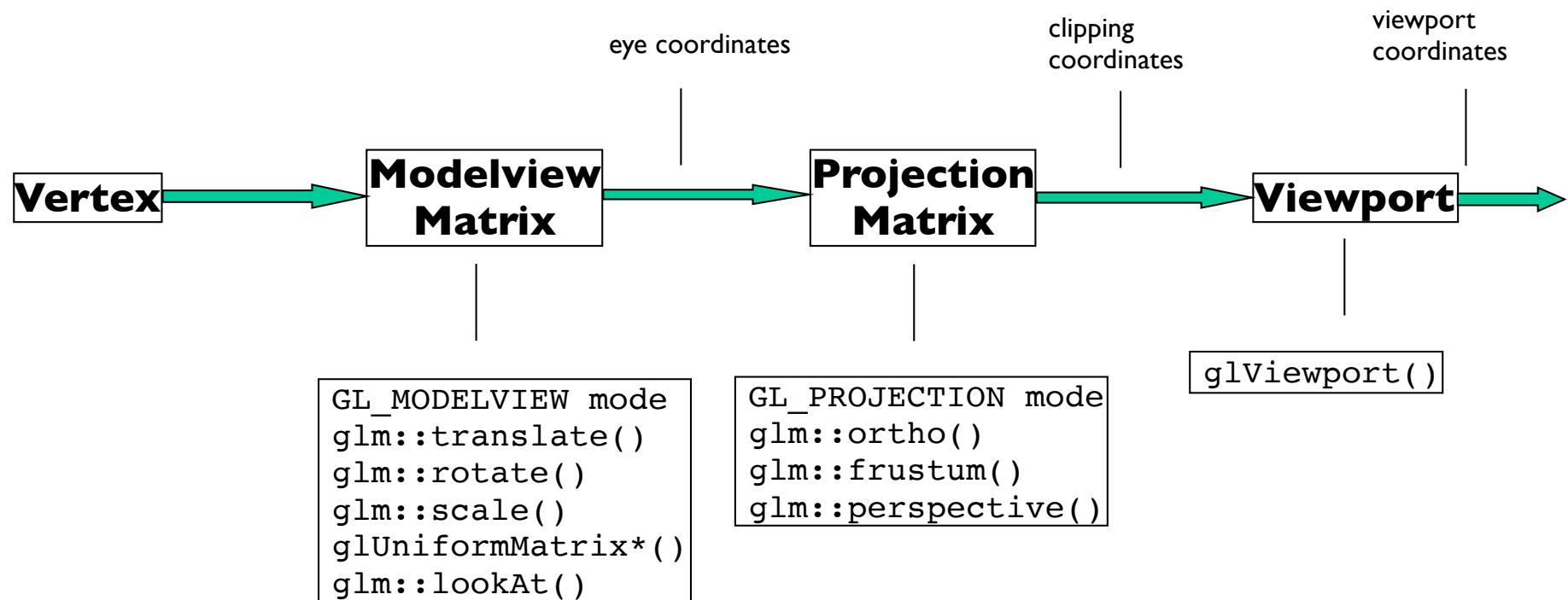
`glm::ortho(left, right, bottom, top)`

- It sets up the 2D scene domain. It is defined by two vertical lines (left and right) and two horizontal lines (bottom and top)
- Default scene domain is $(-1, 1, -1, 1)$.
- It defines the orthogonal projection matrix in 2D.
- Also, it defines the window-viewport transformation in an automated manner.

`glViewport(x, y, width, height)`

- It defines the viewport in the screen window, where (x, y) represent its bottom-left corner, while $(width, height)$ its size.
- By default, the viewport spans the entire domain of screen window.
- There may exist various viewports inside the screen window, which may eventually overlap.

OpenGL graphics pipeline





Example in OpenGL

(using a scene domain and a default viewport)

- In this example, we do not use the default scene domain $(-1, 1, -1, 1)$; that is, the scene domain is given by `glm::ortho(xmin, xmax, ymin, ymax)`
- The function `glViewport(x, y, width, height)` **is not** used explicitly, so the default viewport spans the entire extent of the screen window.

P01, Exercise 3:

Graphics application to draw a house (3 triangles)

```
// Include standard headers
#include <stdio.h>
#include <stdlib.h>

// Include GLEW
#include <GL/glew.h>

// Include GLFW
#include <GLFW/glfw3.h>
GLFWwindow* window;

// GLM header file
#include <glm/glm.hpp>
using namespace glm;

// shaders header file
#include <common/shader.hpp>

// Vertex array object (VAO)
GLuint VertexArrayID;

// Vertex buffer object (VBO)
GLuint vertexbuffer;

// color buffer object (CBO)
GLuint colorbuffer;

// GLSL program from the shaders
GLuint programID;
```

```
// function prototypes
void transferDataToGPUMemory(void);
void cleanupDataFromGPU();
void draw();
```

P01, Exercise 3:

Graphics application to draw a house (3 triangles)

```

int main( void )
{
    // Initialise GLFW
    glfwInit();
    // Setting up OpenGL version and the like
    glfwWindowHint(GLFW_SAMPLES, 4);
    glfwWindowHint(GLFW_CONTEXT_VERSION_MAJOR, 3);
    glfwWindowHint(GLFW_CONTEXT_VERSION_MINOR, 3);
    glfwWindowHint(GLFW_OPENGL_FORWARD_COMPAT, GL_TRUE); // To make MacOS happy; should not be needed
    glfwWindowHint(GLFW_OPENGL_PROFILE, GLFW_OPENGL_CORE_PROFILE);
    // Open a window
    window = glfwCreateWindow( 1024, 768, "House in Red and Green", NULL, NULL);
    // Create window context
    glfwMakeContextCurrent(window);
    // Initialize GLEW
    glewExperimental = true; // Needed for core profile
    glewInit();
    // Ensure we can capture the escape key being pressed below
    glfwSetInputMode(window, GLFW_STICKY_KEYS, GL_TRUE);
    // Dark blue background
    glClearColor(0.0f, 0.0f, 0.4f, 0.0f);
    // transfer my data (vertices, colors, and shaders) to GPU side
    transferDataToGPUmemory();
    // render scene for each frame
    do{
        // drawing callback
        draw();
        // Swap buffers
        glfwSwapBuffers(window);
        // looking for input events
        glfwPollEvents();
    } while (glfwGetKey(window, GLFW_KEY_ESCAPE ) != GLFW_PRESS && glfwWindowShouldClose(window) == 0 );
    // Cleanup VAO, VBOs, and shaders from GPU
    cleanupDataFromGPU();
    // Close OpenGL window and terminate GLFW
    glfwTerminate();
    return 0;
}

```

P01, Exercise 3:

Graphics application to draw a house (3 triangles)

```

void transferDataToGPUmemory(void)
{
    // VAO
    glGenVertexArrays(1, &VertexArrayID);
    glBindVertexArray(VertexArrayID);

    // Create and compile our GLSL program from the shaders
    programID = LoadShaders( "SimpleVertexShader.vertexshader", "SimpleFragmentShader.fragmentshader" );
    // vertices for 2 triangles
    static const GLfloat g_vertex_buffer_data[] = {
        0.0f, 0.0f, 0.0f, 20.0f, 0.0f, 0.0f, 20.0f, 20.0f, 0.0f, // first triangle
        0.0f, 0.0f, 0.0f, 20.0f, 20.0f, 0.0f, 0.0f, 20.0f, 0.0f, // second triangle
        0.0f, 20.0f, 0.0f, 20.0f, 20.0f, 0.0f, 10.0f, 30.0f, 0.0f, // third triangle
    };

    // One color for each vertex
    static const GLfloat g_color_buffer_data[] = {
        1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, // color for 3 vertices of the first triangle
        1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, // color for 3 vertices of the second triangle
        0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, // color for 3 vertices of the third triangle
    };

    // Move vertex data to video memory; specifically to VBO called vertexbuffer
    glGenBuffers(1, &vertexbuffer);
    glBindBuffer(GL_ARRAY_BUFFER, vertexbuffer);
    glBufferData(GL_ARRAY_BUFFER, sizeof(g_vertex_buffer_data), g_vertex_buffer_data, GL_STATIC_DRAW);
    // Move color data to video memory; specifically to CBO called colorbuffer
    glGenBuffers(1, &colorbuffer);
    glBindBuffer(GL_ARRAY_BUFFER, colorbuffer);
    glBufferData(GL_ARRAY_BUFFER, sizeof(g_color_buffer_data), g_color_buffer_data, GL_STATIC_DRAW);
}

```

P01, Exercise 3: Graphics application to draw a house (3 triangles)

```
void cleanupDataFromGPU()
{
    glDeleteBuffers(1, &vertexbuffer);
    glDeleteBuffers(1, &colorbuffer);
    glDeleteVertexArrays(1, &VertexArrayID);
    glDeleteProgram(programID);
}
```

P01, Exercise 3:

Graphics application to draw a house (3 triangles)

```
void draw (void)
{
    // Clear the screen
    glClear( GL_COLOR_BUFFER_BIT );
    // Use our shader
    glUseProgram(programID);

    // window-viewport transformation
    glm::mat4 mvp = glm::ortho(-40.0f, 40.0f, -40.0f, 40.0f);
    // retrieve the matrix uniform locations
    unsigned int matrix = glGetUniformLocation(programID, "mvp");
    glUniformMatrix4fv(matrix, 1, GL_FALSE, &mvp[0][0]);

    // 1st attribute buffer : vertices
    glEnableVertexAttribArray(0);
    glBindBuffer(GL_ARRAY_BUFFER, vertexbuffer);
    glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, 0, (void*)0);

    // 2nd attribute buffer : colors
    glEnableVertexAttribArray(1);
    glBindBuffer(GL_ARRAY_BUFFER, colorbuffer);
    glVertexAttribPointer(1, 3, GL_FLOAT, GL_FALSE, 0, (void*)0);

    // Draw the 3 triangles !
    glDrawArrays(GL_TRIANGLES, 0, 9); // 9 indices starting at 0

    // Disable arrays of attributes for vertices
    glDisableVertexAttribArray(0);
    glDisableVertexAttribArray(1);
}
```


P01, Exercise 3:

Graphics application to draw a house (3 triangles)

vertexshader.vs

```
#version 330 core

// Input vertex data and color data
layout(location = 0) in vec3 vertexPosition;
layout(location = 1) in vec3 vertexColor;

// window-viewport transformation matrix
uniform mat4 mvp;

// Output fragment data
out vec3 fragmentColor;

void main()
{
    // project each vertex in homogeneous coordinates
    gl_Position = mvp * vec4(vertexPosition, 1.0);

    // the vertex shader just passes the color to fragment shader
    fragmentColor = vertexColor;
}
```

P01, Exercise 3:

Graphics application to draw a house (3 triangles)

fragmentshader.fs

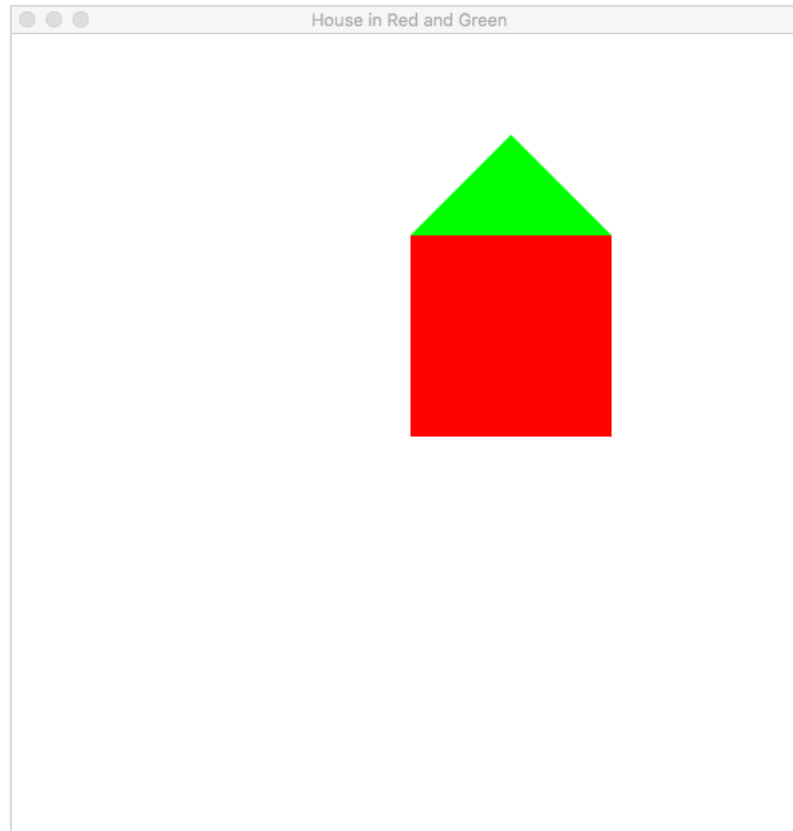
```
#version 330 core

// Interpolated values from the vertex shaders
in vec3 fragmentColor;

// Output data
out vec3 color;

void main()
{
    color = fragmentColor;
}
```

P01, Exercise 3: Graphics application to draw a house (3 triangles)





Example in OpenGL

(using a scene domain and 4 viewports)

- In this example, we use a specific scene domain given by `glm::ortho(xmin,xmax,ymin,ymax)`
- The function `glViewport(x, y, width, height)` **is** used explicitly to define each viewport inside the screen window.
- This program takes advantage of the same shaders as the previous program.

Graphics application to draw the same house in 4 viewports

```
// Include standard headers
#include <stdio.h>
#include <stdlib.h>

// Include GLEW
#include <GL/glew.h>

// Include GLFW
#include <GLFW/glfw3.h>
GLFWwindow* window;

// GLM header file
#include <glm/glm.hpp>
using namespace glm;

// shaders header file
#include <common/shader.hpp>

// Vertex array object (VAO)
GLuint VertexArrayID;

// Vertex buffer object (VBO)
GLuint vertexbuffer;

// color buffer object (CBO)
GLuint colorbuffer;

// GLSL program from the shaders
GLuint programID;

// screen window
GLint WindowWidth = 600;
GLint WindowHeight = 600;

// function prototypes
void transferDataToGPUMemory(void);
void cleanupDataFromGPU();
void draw();
```

Graphics application to draw the same house in 4 viewports

```
int main( void )
{
    // Initialise GLFW
    glfwInit();

    // Setting up OpenGL version and the like
    glfwWindowHint(GLFW_SAMPLES, 4);
    glfwWindowHint(GLFW_CONTEXT_VERSION_MAJOR, 3);
    glfwWindowHint(GLFW_CONTEXT_VERSION_MINOR, 3);
    glfwWindowHint(GLFW_OPENGL_FORWARD_COMPAT, GL_TRUE); // To make MacOS happy; should not be needed
    glfwWindowHint(GLFW_OPENGL_PROFILE, GLFW_OPENGL_CORE_PROFILE);

    // Open a window
    window = glfwCreateWindow( 1024, 768, "House in 4 Viewports", NULL, NULL);

    // Create window context
    glfwMakeContextCurrent(window);

    // Initialize GLEW
    glewExperimental = true; // Needed for core profile
    glewInit();

    // Ensure we can capture the escape key being pressed below
    glfwSetInputMode(window, GLFW_STICKY_KEYS, GL_TRUE);

    // White background
    glClearColor(1.0f, 1.0f, 1.0f, 0.0f);

    // Clear the screen
    glClear( GL_COLOR_BUFFER_BIT );

    // transfer my data (vertices, colors, and shaders) to GPU side
    transferDataToGPUmemory();

    // see next page for more ...
}
```

Graphics application to draw the same house in 4 viewports

```
// Create a framebuffer for viewports
GLuint FramebufferName = 0;
glGenFramebuffers(1, &FramebufferName);

// render scene for each frame
do{ //left bottom
    glBindFramebuffer(GL_FRAMEBUFFER, 0);
    glViewport(0, 0, WindowWidth*0.5, WindowHeight*0.5);
    draw();
    //right bottom
    glViewport(WindowWidth*0.5, 0, WindowWidth*0.5, WindowHeight*0.5);
    draw();
    //left top
    glViewport(0, WindowHeight*0.5, WindowWidth*0.5, WindowHeight*0.5);
    draw();
    //right top
    glViewport(WindowWidth*0.5, WindowHeight*0.5, WindowWidth*0.5, WindowHeight*0.5);
    draw();
    // Swap buffers
    glfwSwapBuffers(window);
    // looking for input events
    glfwPollEvents();
} while (glfwGetKey(window, GLFW_KEY_ESCAPE) != GLFW_PRESS && glfwWindowShouldClose(window) == 0);

// delete framebuffer
glDeleteFramebuffers(1,&FramebufferName);

// Cleanup VAO, VBOs, and shaders from GPU
cleanupDataFromGPU();

// Close OpenGL window and terminate GLFW
glfwTerminate();
return 0;
}
```

Graphics application to draw the same house in 4 viewports

```

void transferDataToGPUmemory(void)
{
    // VAO
    glGenVertexArrays(1, &VertexArrayID);
    glBindVertexArray(VertexArrayID);

    // Create and compile our GLSL program from the shaders
    programID = LoadShaders( "SimpleVertexShader.vertexshader", "SimpleFragmentShader.fragmentshader" );
    // vertices for 2 triangles
    static const GLfloat g_vertex_buffer_data[] = {
        0.0f, 0.0f, 0.0f, 20.0f, 0.0f, 0.0f, 20.0f, 20.0f, 0.0f, // first triangle
        0.0f, 0.0f, 0.0f, 20.0f, 20.0f, 0.0f, 0.0f, 20.0f, 0.0f, // second triangle
        0.0f, 20.0f, 0.0f, 20.0f, 20.0f, 0.0f, 10.0f, 30.0f, 0.0f, // third triangle
    };

    // One color for each vertex
    static const GLfloat g_color_buffer_data[] = {
        1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, // color for 3 vertices of the first triangle
        1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, // color for 3 vertices of the second triangle
        0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, 0.0f, 1.0f, 0.0f, // color for 3 vertices of the third triangle
    };

    // Move vertex data to video memory; specifically to VBO called vertexbuffer
    glGenBuffers(1, &vertexbuffer);
    glBindBuffer(GL_ARRAY_BUFFER, vertexbuffer);
    glBufferData(GL_ARRAY_BUFFER, sizeof(g_vertex_buffer_data), g_vertex_buffer_data, GL_STATIC_DRAW);
    // Move color data to video memory; specifically to CBO called colorbuffer
    glGenBuffers(1, &colorbuffer);
    glBindBuffer(GL_ARRAY_BUFFER, colorbuffer);
    glBufferData(GL_ARRAY_BUFFER, sizeof(g_color_buffer_data), g_color_buffer_data, GL_STATIC_DRAW);
}

```


Graphics application to draw the same house in 4 viewports

```
void cleanupDataFromGPU()
{
    glDeleteBuffers(1, &vertexbuffer);
    glDeleteBuffers(1, &colorbuffer);
    glDeleteVertexArrays(1, &VertexArrayID);
    glDeleteProgram(programID);
}
```

Graphics application to draw the same house in 4 viewports

```
void draw (void)
{
    // Clear the screen : this has been moved to main(); otherwise only one house is displayed
    // glClear( GL_COLOR_BUFFER_BIT );

    // Use our shader
    glUseProgram(programID);

    // window-viewport transformation
    glm::mat4 mvp = glm::ortho(-40.0f, 40.0f, -40.0f, 40.0f);
    // retrieve the matrix uniform locations
    unsigned int matrix = glGetUniformLocation(programID, "mvp");
    glUniformMatrix4fv(matrix, 1, GL_FALSE, &mvp[0][0]);

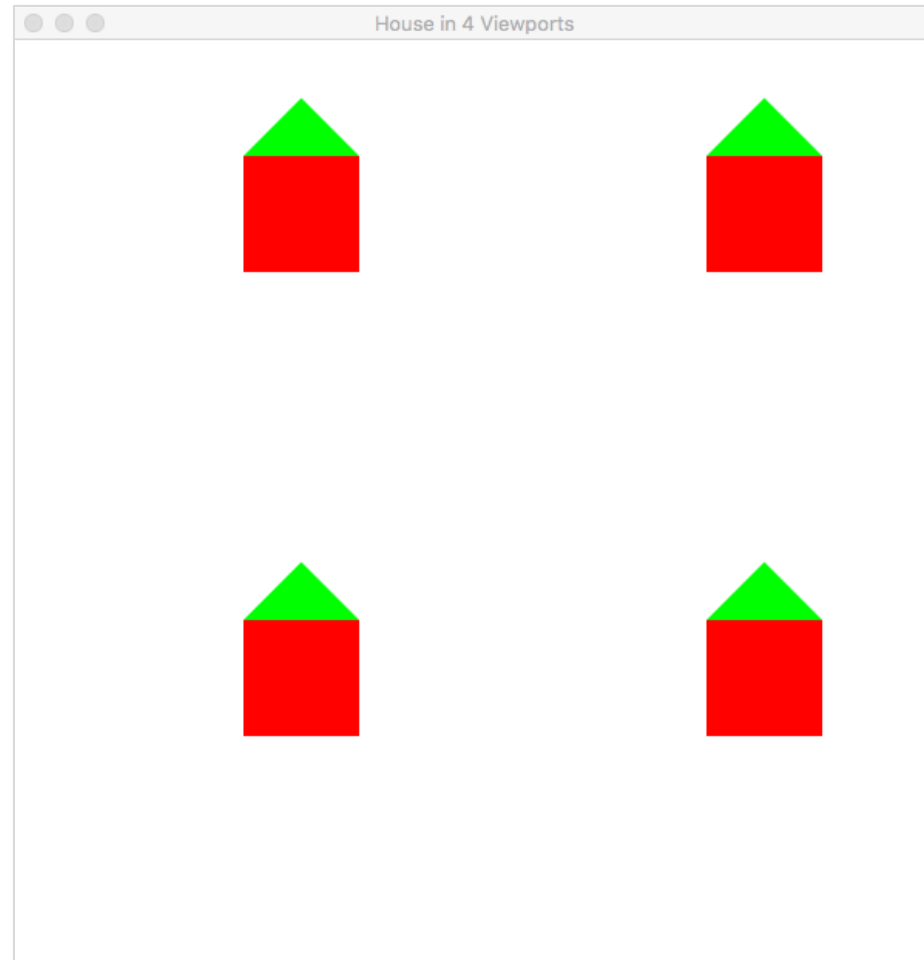
    // 1st attribute buffer : vertices
    glEnableVertexAttribArray(0);
    glBindBuffer(GL_ARRAY_BUFFER, vertexbuffer);
    glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, 0, (void*)0);

    // 2nd attribute buffer : colors
    glEnableVertexAttribArray(1);
    glBindBuffer(GL_ARRAY_BUFFER, colorbuffer);
    glVertexAttribPointer(1, 3, GL_FLOAT, GL_FALSE, 0, (void*)0);

    // Draw the 3 triangles !
    glDrawArrays(GL_TRIANGLES, 0, 9); // 9 indices starting at 0

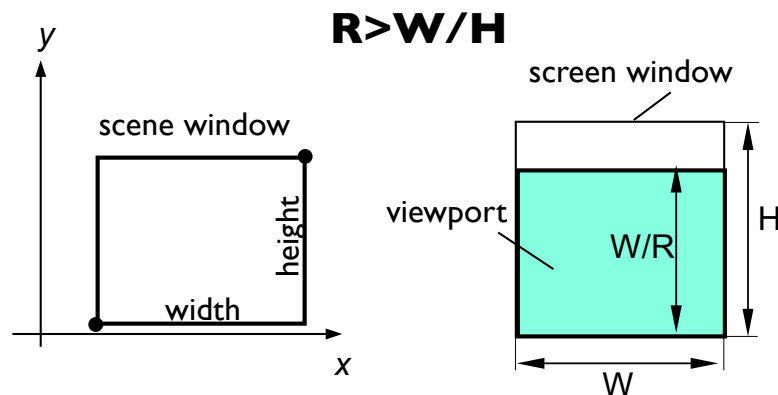
    // Disable arrays of attributes for vertices
    glDisableVertexAttribArray(0);
    glDisableVertexAttribArray(1);
}
```

Graphics application to draw the same house in 4 viewports



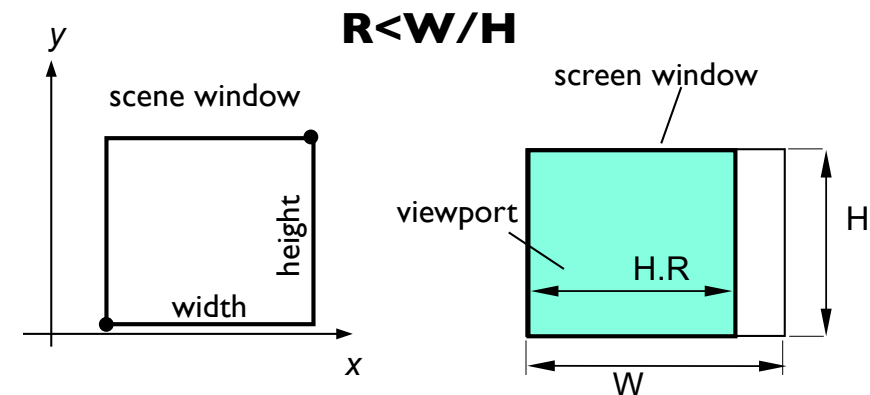
Automated setup of the viewport without image distortion

- $R = \text{aspect ratio of the scene domain or window} = \text{width} / \text{height}$
- We consider two cases:



- To avoid image distortion, a rectangular region on the top of screen window will be discarded.
- Thus, the mapped image will own the resolution $W \times W/R$.

`glViewport(0,0,W,W/R);`



- To avoid image distortion, a rectangular region on the right-hand side of screen window will be discarded.
- Thus, the mapped image will own the resolution $H * R \times H$.

`glViewport(0,0,H*R,H);`



Summary:

....:

- Basic definitions in 2D:
 - Global coordinates (scene domain): continuous domain
 - Screen coordinates (image domain): discrete domain
- Window-viewport transformation
- Window-viewport transformation in OpenGL
- Geometric transformations in OpenGL/GLM
- Graphics pipeline (or rendering pipeline)
- Mapping a scene into various viewports
- Avoiding image distortion
- OpenGL examples